# Efficient Star Identification Algorithm for Nanosatellites in Harsh Environment IAA-AAS-CU-17-05-02 <br> Vincenzo Schiattarella ${ }^{1}$, Dario Spiller ${ }^{2}$, Fabio Curt $\beta^{3}$ 

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## Introduction

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This work proposes a feasibility study for a third improvement of the Multi-Poles Algorithm (MPA).

The MPA is a star identification algorithm for Lost in Space.
It is especially designed to be robust in presence of a large number of false objects in the image.

## Multi-Poles Algorithm

## Original Idea

The original idea has been published in Advances in Space Research, Vol. 59, Issue 8, Pages 2133-2147, "A novel star identification technique robust to high presence of false objects: The Multi-Poles Algorithm"

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> Recognize stars using THREE phases
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## MPA main characteristics:

> Recognize stars using THREE phases
> Magnitude data are NOT required

- Stop when the desired number of stars are recognized

MPA is able to return correct identifications for a number of false objects up to 6 times the number of the cataloged stars in the image.

## Multi-Poles Algorithm

## Participation to ESA contest - Star Trackers: First Contact

Goal: Propose new and fast star identification algorithms for star trackers that are robust to measurement uncertainties and artifacts.


Star Trackers: First Contact

Lost in Space

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> Recognize stars using TWO phases
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## Star Trackers: First Contact

Lost in Space

Ended Sept. 1, 2017

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MPA has reported the second highest accuracy score and speed:

- 9703.4313 (w.r.t. a perfect score of 9921.0 )
- 0.58 s (Total time required for 10000 scenes) $58 \mu \mathrm{~s}$ per scene



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## Multi-Poles Algorithm

## New version

The new MPA is a mixed approach between the two former versions of the algorithm:
> Recognize stars using TWO phases: the acceptance phase and the check phase.
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> Magnitude data are REQUIRED
$\rightarrow$ Stop when the desired number of stars are recognized
The on-board catalog is based on the Hipparcos identifier $h$ and the magnitude $m$ of 2 stars.

| $h_{01}$ | $h_{02}$ | $m_{01}$ | $m_{02}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $h_{11}$ | $h_{12}$ | $m_{11}$ | $m_{12}$ |  |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |  |
| on-board catalog |  |  |  |  |

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First of all a function to project spikes image coordinates onto sensor reference frame is required. Each spike will be associated to a 3D unit vector $\boldsymbol{v}_{i}$ and an estimated magnitude value $m_{i}$.

$$
\boldsymbol{s}_{\boldsymbol{i}}=\left[\boldsymbol{v}_{i}, m_{i}\right] \quad \text { Sorted by ascending magnitude }
$$

## Multi-Poles Algorithm

## Acceptance phase

The acceptance phase is based on a polar approach and returns a set of Accepted stars. This phase consists of the following steps:

1. Select a spike $s_{i}$ named pole $p^{(i)}$, and computes the angular distances $\theta_{i j}$ between the pole and the other spikes $s_{j}$ in the image, named neighbors $n_{j}^{(i)}$.


Image

## Multi-Poles Algorithm

## Acceptance phase

2. Search for each angular distance $\theta_{i j}$ within a given tolerance the stars in the onboard catalog.

| $h_{01}$ | $h_{02}$ | $m_{01}$ | $m_{02}$ |
| :---: | :---: | :---: | :---: |
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| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| $h_{11}$ | $h_{12}$ | $m_{11}$ | $m_{12}$ |
| $\vdots$ |  |  |  |
| Search |  |  |  |
| result |  |  |  |

on-board catalog

## Multi-Poles Algorithm

## Acceptance phase

2. Search for each angular distance $\theta_{i j}$ within a given tolerance the stars in the onboard catalog.

3. Restrict the number of resulting stars through magnitude information making lists of stars pairs Hipparcos identifiers $\prod_{j}^{(i)}$.
The pairs are the admissible pole's and neighbors' identifiers.

## Multi-Poles Algorithm

## Acceptance phase

3. Accept as Pole Star the Hipparcos identifier which has the maximum number of appearances through the lists of pairs.

| $\prod_{2}^{(1)}$ | $\prod_{3}^{(1)}$ | $\Pi_{4}^{(1)}$ | $\prod_{5}^{(1)}$ | $\prod_{6}^{(1)}$ | $\Pi_{7}^{(1)}$ | $\prod_{8}^{(1)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 31,40 | 100,102 | 1346,1352 | $5, \underline{10}$ | 81,97 | 993,999 | 534,546 |
| 500,512 | $\underline{10,16}$ | 416,425 | 44,65 |  | 2023,2031 | 876,893 |
|  | 231,242 | $8, \underline{10}$ |  |  | 3648,3742 |  |
|  | 1028,1032 |  |  |  | 10,21 |  |

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4. Search in the lists of pairs the Hipparcos identifier coupled with Pole Star and accept it as Neighbor Star. The Accepted stars set will be:

| $p^{*(1)}$ | $F$ | $n_{3}^{*(1)}$ | $n_{4}^{*(1)}$ | $n_{5}^{*(1)}$ | $F$ | $F$ | $n_{8}^{*(1)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | -1 | 16 | 8 | 5 | -1 | -1 | 21 |

## Multi-Poles Algorithm

## Next poles selection

| $n_{8}^{*(1)}$ | $\bullet-1$ | $\bullet n_{5}^{*(1)}$ |
| :---: | :---: | :---: |
| $\bullet^{-1}$ | -1 | $\bullet n_{4}^{*(1)}$ |
|  | $n_{3}^{*(1)} \bullet$ | $p^{*(1)}$ |



## Accepted stars returned

New poles are selected within the spikes previously accepted as neighbor stars.

## Multi-Poles Algorithm

## Next poles selection



## Accepted stars returned

New poles are selected within the spikes previously accepted as neighbor stars.

Accepted stars NOT returned
Selection criterion remains spike magnitude: next spike is selected as pole.

## Multi-Poles Algorithm

## Check phase

The check phase performs a cross-check between two sets of accepted stars. Check if the number of stars belonging to the intersection of two accepted stars sets is greater than a threshold value $t^{*}$, which is an user defined minimum number of required stars.

| $p^{*(1)}$ | $F$ | $n_{3}^{*(1)}$ | $n_{4}^{*(1)}$ | $n_{5}^{*(1)}$ | $F$ | $F$ | $n_{8}^{*(1)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | -1 | 16 | 8 | 5 | -1 | -1 | 21 |

First accepted stars set

| $n_{1}^{*(3)}$ | $F$ | $p^{*(3)}$ | $n_{4}^{*(3)}$ | $F$ | $n_{6}^{*(3)}$ | $F$ | $n_{8}^{*(3)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | -1 | 16 | 8 | -1 | 11 | -1 | 21 |

Second accepted stars set

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| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | -1 | 16 | 8 | -1 | 11 | -1 | 21 |

Second accepted stars set

| $s_{1}$ | $s_{2}$ | $s_{3}$ | $s_{4}$ | $s_{5}$ | $s_{6}$ | $s_{7}$ | $s_{8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | -1 | 16 | 8 | -1 | -1 | -1 | 21 |

Recognized stars set

## Results

## Tests Definition

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We perform the following simulation campaigns:
> Tests for increasing number of false objects
> Tests with at least $\boldsymbol{\eta}$ real stars in the image
> Tests with only $\boldsymbol{\eta}$ real stars in the image

## Results for increasing number of false objects in the image

The simulation campaign deals with tests performed for ascending maximum number of false objects in the image. For each simulation, 1000 images with random pointings have been checked. The number of actual stars per image is at least 0 (i.e. the most generic conditions).


Maximum false stars in the image


## Results with at least $\eta$ real stars in the image

Defining $\eta$ as the minimum value of actual stars in the image, the simulation campaign deals with tests performed for ascending $\boldsymbol{\eta}$ ranging from 0 to 9 stars. For each simulation, 1000 images with random attitude have been checked.



## Results with only $\eta$ real stars in the image

Defining $\boldsymbol{\eta}$ as the value of actual stars in the image, the simulation campaign deals with tests performed for ascending $\eta$ ranging from 2 to 9 stars.
For each simulation, 1000 images with random attitude have been checked.



## Results

## Time Performances

The MPA C source code has been profiled on an Intel® Core 2 Quad Processor Q6600 @ 2.40 GHz machine CPU architecture.

The elapsed time for simulation depends on number of stars in the image.




## Conclusion

The results show that MPA success rate ranges from $99 \%$ to $100 \%$ for simulation with at least 3 actual stars per image. In case with less than 3 actual stars in the image no wrong identification has occurred.

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With a low computational performances CPU architecture, the mean elapsed time for random simulations ranges from a minimum of $3 \cdot 10^{-5}$ seconds with 10 false stars to a maximum of $2.7 \cdot 10^{-4}$ seconds with 80 false stars.

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Future improvements will require increasing centroiding noise and finding best parameters configuration.

## Thanks for your attention.

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